

Previous Lecture

- Populations are Structured
- Basic descriptive attributes of populations:
 - Density (+estimation techniques; quadrat/mark-recapture)
 - Distribution
 - Dispersion (+estimation technique; index of dispersion):
- Practice Problem Video on Mark-Recapture on website.

Lecture 2

All Populations Potentially Grow Exponentially

A. Exponential population growth* (Smith&Smith Chapter 9)

B. Next: Exponential growth modified by age structure (next time; S&S Chap. 9)

*Faite attention! Exponential growth theory is one of the most important concepts in all of ~~Ecology~~ Ecology/science!

Exponential Growth

♦The ‘Law of Exponential Growth’ is the

♦Where does this law come from?

Exponential Growth

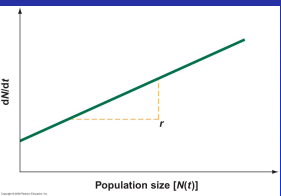
- Individuals have some maximum birth rate (b)
- Individuals have some minimum death rate (d)
- The “per capita population growth rate”, r , is _____

Exponential Growth

- Total rate = per capita rate * capitas
- Population growth rate (dN/dt):

Exponential Growth

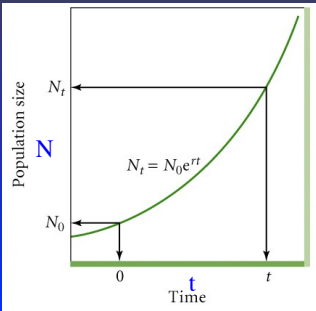
- This is an equation for a line, whose slope is r :



Exponential Growth

→ BUT, what kind of population growth (**N** vs. **time**) is predicted by this equation?

N vs. time



Population size N

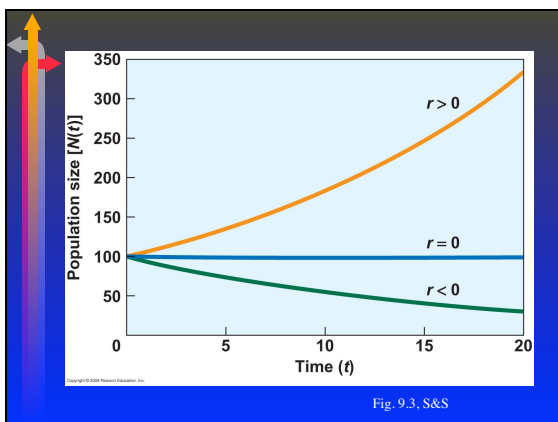
Time t

$N_t = N_0 e^{rt}$

N_t

N_0

0 t



Version 2 of the exponential growth equation replaces e^r with a different constant

Real World Exponential Growth



(a)



(b)

Fig. 9.6, S&S

Real World Exponential Growth

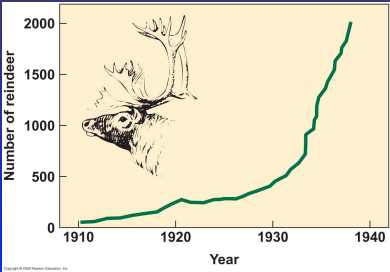
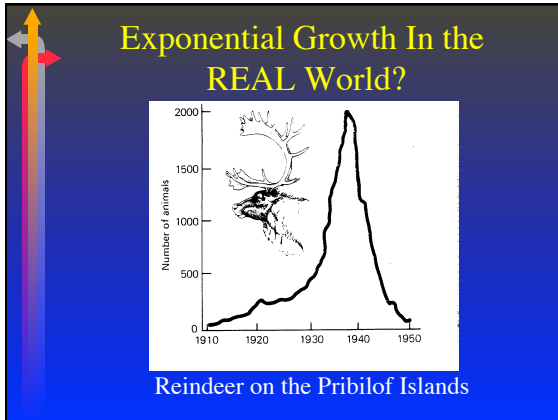


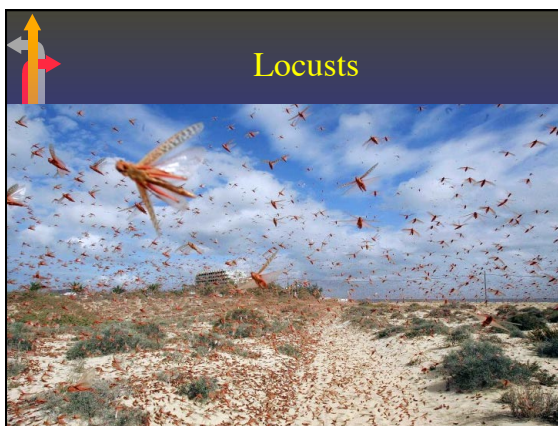
Fig. 9.5, S&S

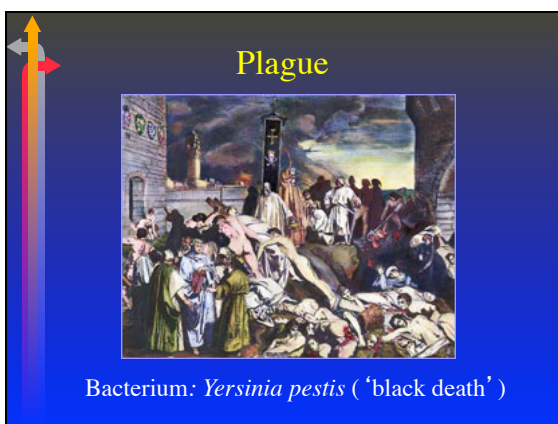


- Realized Exponential Growth**
- Rabbits in Australia
 - Gypsy moth in North America
 - Locusts in Africa
 - Plague in Europe
 - Lemmings in the Arctic
 - Etc...










Bacterium: *Yersinia pestis* ('black death')



Lemmings




Sample Problem

→ *E. coli* cells propagate by binary fission. They don't 'give birth' in the traditional sense. However, if the effective 'birth rate' of these cells is 6 cells/cell*hr, and death rate is 0, and the initial population consists of 100 cells, how long would it take to reach a population size of 4.92×10^{43} cells, enough to cover planet Earth 1 meter deep in bacteria?


→ SEE PRACTICE PROBLEM VIDEO 2!



Another sample problem!


→ If you wanted to leave \$1,000,000 to one grandchild in 60 years, how much would your initial investment have to be in order to accomplish this, assuming a 10% continuously compounded interest rate?

→ SEE PRACTICE PROBLEM VIDEO 2!



Another thought problem

- Facts: A penny is 19.05 mm in diameter. A penny is 1.52 mm thick. It is 384,400 km to the moon. I start stacking pennies in adjacent stacks (in a single row of stacks). The first stack has 1 penny, the second, 2, the third, 4, etc., doubling each time.
- How wide would row of penny stacks be when the last stack reaches to the moon?



Summary

- All populations potentially grow exponentially
- Exponential growth is a “compound interest” phenomenon
- Occasional “outbursts” of exponential growth do occur in nature
