### Lecture 5 - Density Dependence

- Reading/Watching: Smith & Smith Chap. 11, VideoIntro5 (Bio. 221 web site)
- ➡ Fitness
- Assumptions of the logistic
- Problem solving with the logistic
- Implications of the theory
- Density-dependence in plants
- General importance of density-dependence



An individual has a high fitness if: A) it has the most mates B) it leaves the most offspring, C) it survives the best, D) it can lift the most weights, E) none of the above



### **Propensity fitness**

- Fitness is a property of the individual
- Fitness should measure the rate at which that individual's genes are propagated
- The **propensity fitness** is the expected 'population growth rate of the individual', where  $\lambda$  is measured for a matrix constructed for each individual in the population

### Propensity fitness

We determine an **individual's** propensity to produce a certain number of offspring at each age and to survive at each age, then fill in the traditional matrix:

#### Fitness

- → Because  $\lambda^{(i)}$  is determined by the eigenvalue of the matrix A<sup>(i)</sup>, we see that:
  - Fitness depends on the probability of survival
  - -Fitness depends on the amount of reproduction
  - Fitness depends on the timing of that reproduction



## Limits on Population Growth

There must be limits to exponential growth
 (projections of exponential growth are eventually, inevitably, wrong)

- Two classes of 'checks' on population growth
  Density-independent factors
  - -Density-dependent factors\* (b, d are functions of N)

## Density-dependent theory

Logistic population growth - a parsimonious approach

'Parsimony' - characterized by frugality; sparing; using extreme economy





## r as a function of N (cont' d)

- With logistic growth, r declines with increasing N in a linear fashion
- $\rightarrow$  Let the maximum r = r<sub>max</sub>
- Let the N where r=0 be called K (carrying capacity)

# Why does r decline as N increases?

- → b declines as N increases.
- ➡d goes up as N increases.
- ₩r=b-d!



















## Logistic Population Growth

- Logistic population growth is sigmoidal (if initial N<K)</p>
- Population size approaches K asymptotically
- ➡Population size increases to K if N<K
- ➡Population size decreases to K if N>K



Integrated form of the logistic equation:

## Assumptions\* of the Logistic

- All individuals reduce growth rate equally
- ➡r<sub>max</sub> and K are constants
- No time lag in response of dN/dt to changing N
- \*Note: All assumptions questionable for some (most?) organisms in some (most?) environments



















































# Theory vs. Real World

- r may not decline linearly with increasing N
  Allee effect at low densities
  - →no competition until a threshold
- ➡K certainly varies with the environment
- Time lags in population response to density occur















Siberian Tiger

Characterized by: -late reproduction -low offspring numbers -slow maturation

#### Caution

- Most species (even 'r-selected' species) will experience some density dependence at some N
- 'K-selected' species go through periods where their dN/dt is not limited by density.
- r and K are theoretical constructs
- Numerous factors other than density affect selection on life history traits

## Density-dependence in plants

 There is a law that describes densitydependence in plants: it is NOT logistic.
 -3/2 thinning rule:









## Summary

Logistic theory predicts that populations have some maximum sustainable N (=K) due to resource limitation

Logistic theory can make predictions about the real world, such as the prey population size that would be optimal for a prudent predator

#### Sample Problem 4 u off recent midterm

A population of coyotes has taken up residency at Coopers Rock State Forest. Predation, hunting, and car accidents have minimal effect on the coyote population dynamics. In addition, since wolves and mountain lions are long gone from Coopers Rock, they are the 'top dog' (apex) carnivore. But coyotes do respond to their own densities with territoriality in order to defend resources, so there is a limit to the maximum sustainable population size.

- 1. Which equation would govern the rate of change of population size, given the scenario described above?
- 2. If the maximum sustainable N for coyotes at Coopers Rock is 100, the current population size is 10, and r<sub>max</sub> is 0.5, how fast is the population growing?
  (A) 2.5, (B) 4.5, (C) 6.3, (D) 12.5, (E) 50.0
- 3. Theoretically, how long would it take the coyote population to reach its carrying capacity? (A) 22 y, (B) 47 y, (C) 79 y, (D) 1.028 y, (E) an infinite number of years; the population size approaches K asymptotically.

### Next Lecture

→IV. Population Dynamics ➡D. Interspecific competition S&S Chapter 13